

AGS Complex Machine Studies (AGS Studies Report No. 289) Stopband Correction of the AGS Booster Integer Coupling ($Q_x + Q_y = 9$) Correction Data				
Study Period: April 1, 11, 23, 1993				
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Machine: April 01: User3 10 Turns Low dB/dt Injection April 11: User1 5 Turns High dB/dt Injection April 23: User3 5 Turns 1.7 kG dB/dt=0 Porch				
Aim: Correction of the integer coupling sum resonance $Q_x + Q_y = 9$.				

All data points on $Q_x + Q_y = 9$ correction currents; $N(\cos 9XY)$ and $N(\sin 9XY)$ are listed in Table I.

Table I $Q_x + Q_y = 9$ correction current data list.

date						crossing	residual
T	B	dB/dt	dRset	N(cos9XY)	N(sin9XY)	speed	loss(%)
(ms)	(kG)	(G/ms)	(cm)			(dQ/ms)	/cross
							times
last year [Gardner, AGS SR-273]							
	3.6	0	?	290	90		
Apr.01	u3	10turns		Qy=4.6 fix, change Qx			
40	1.62	20	?	10 ± 5	25 ± 5	0.01	9/?
61	2.89	72	?	-120 ± 10	240 ± 10	?	8/?

Apr.11	u1	5t	Qx,Qy= 4.44,4.62 --> 4.38 4.56				
35	1.80	70	?	130 \pm 15	-60 \pm 15	?	29 /?
55	3.34	70	?	190 \pm 20	-30 \pm 10	?	38 /?
75	4.74	70	?	275 \pm 15	20 \pm 10	?	5 /?
88	5.25	33	?	295 \pm 10	35 \pm 10	?	0.6/?

Apr.23	u3	Qy=4.6	All sextupole = 0 A, Dump Bump = OFF				
80	1.7	0	-0.4	-65 \pm 5	54 \pm 5	0.014	32/?
			0.4	-48 \pm 2	39 \pm 1		29/?
			1.2	-38 \pm 2	32 \pm 2		22/?

I B and dB/dt Dependence

B and dB/dt dependence of correction currents; $N(\cos 9XY)$ and $N(\sin 9XY)$ were measured on April 11. The data points were fitted with functions;

$$\begin{aligned} N(\cos 9XY) &= Co + Cb B + Cbt \, dB/dt \\ N(\sin 9XY) &= So + Sb B + Sbt \, dB/dt . \end{aligned} \quad (1)$$

Here Co , Cb , Cbt , So , Sb and Sbt were fitting parameters. The unit of B and dB/dt were kG and G/ms=kG/s, respectively. The result were;

$$\begin{aligned} Co &= 35 \pm 55 & So &= -111 \pm 45 \\ Cb &= 49.2 \pm 7.2 & Sb &= 28.5 \pm 6.0 \\ Cbt &= 0.04 \pm 0.53 & Sbt &= -0.11 \pm 0.41 \\ X^2 &= 0.50 & X^2 &= 0.79 \end{aligned} \quad (2)$$

The correction currents has off-set term (remanent field) and B term (magnet construction and alignment) but less dB/dt term (eddy current and back-leg windings). The dB/dt term $N(\cos 0XY)$, correction current for $Qx-Qy=0$, was also negligibly small after the change of C5 back-leg winding [W. Van Asselt, AGS schedule meeting]. Then we conclude that there are negligibly small skew quadrupole errors which are proportional to dB/dt .

II Dependence on dR

On April 23 dR (momentum change) dependence of $N(\cos 9XY)$ and $N(\sin 9XY)$ were measured on the $dB/dt=0$ porch. The data points, listed in Table I, were fitted with functions;

$$\begin{aligned} N(\cos 9XY) &= Co + Cr \, dR_{set} \\ N(\sin 9XY) &= So + Sr \, dR_{set}. \end{aligned} \quad (3)$$

The results were:

$$\begin{aligned} Co &= -55.2 \pm 2.4 & So &= 43.7 \pm 1.6 \\ Cr &= 14.8 \pm 2.8 & Sr &= -10.6 \pm 2.5 \\ X^2 &= 1.09 & X^2 &= 1.94 \end{aligned} \quad (4)$$

The linear fits (3) were not so bad. The results show the existence of dR dependent term, which explains the residual loss of $Q_x+Q_y=9$ correction. We need $(6n-3)$ th skew sextupole strings to cancel Cr and Sr.

III Consistency of Each Data Point

We calculated the correction currents from the parameters (2) for the B and dB/dt on April 1 and at the fit (4). We also calculated the correction currents from the parameters (4) for $dR_{set}=0.4\text{cm}$. They are listed and compared with the measured currents in Table II.

Table II Consistency of each data points.

B (kG)	1.62	2.89	1.7
dB/dt (G/ms)	20	72	0
measured on April 1			
$N(\cos 9XY)$	10 ± 5	-120 ± 10	
$N(\sin 9XY)$	25 ± 5	240 ± 10	
calculated from (4); $dR_{set}=0.4$			
$N(\cos 9XY)$			-49 ± 3
$N(\sin 9XY)$			48 ± 2
calculated from (2)			
$N(\cos 9XY)$	115 ± 57	180 ± 70	84 ± 57
$N(\sin 9XY)$	-67 ± 47	-37 ± 57	-63 ± 47
change of dB/dt term			
$\delta N(\cos 9XY)/\delta(dB/dt)$	-5.3 ± 2.9	-4.2 ± 1.0	
$\delta N(\sin 9XY)/\delta(dB/dt)$	4.6 ± 2.4	3.8 ± 0.8	

The inconsistency of parameters (2) and data points measured on April 1 is explained by the change of C5 back-leg winding, which might have changed the dB/dt term. The difference between measured and calculated were divided by dB/dt. The results were listed in the bottom of Table II. The data at B=1.62kG, dB/dt=20G/ms and the data at B=2.89kG, dB/dt=70G/ms gave the same values within the errors. And the phase of dB/dt term; $\delta N(\sin 9XY)/\delta N(\cos 9XY)$, which was the ratio of $\delta N(\sin 9XY)/\delta (dB/dt)$ and $\delta N(\cos 9XY)/\delta (dB/dt)$, was

$$\delta N(\sin 9XY)/\delta N(\cos 9XY) = -0.89 \pm 0.29 . \quad (5)$$

This value is close to the calculated phase of C5 back-leg winding;

$$\delta N(\sin 9XY)/\delta N(\cos 9XY) = -0.5 .$$

The change was proportional to dB/dt and was on the phase of C5 back-leg winding.

The inconsistency of parameters (2) and (4) can not be explained. If we assume dRset=10cm two results meet each other. But dRset could not be such a large value. The chromaticities and orbits were not the same for these two cases. But we are not sure whether these could have changed the correction current.